

If  $f''(x) > 0$  on an open interval  $(a, b)$ , then which of the following statement is correct?

- ▶  $f$  is concave up on  $(a, b)$ .
- ▶  $f$  is concave down on  $(a, b)$ .
- ▶  $f$  is linear on  $(a, b)$ .

If  $x > 0$  then  $\frac{d}{dx}[\ln x] =$  \_\_\_\_\_

- ▶ 1
- ▶  $x$
- ▶  $\frac{1}{x}$
- ▶  $\ln \frac{1}{x}$

Let  $y = (x^3 + 2x)^{37}$ . Which of the following is correct?

- ▶  $\frac{dy}{dx} = (37)(x^3 + 2x)^{36}$
- ▶  $\frac{dy}{dx} = 111x^2(x^3 + 2x)^{36}$

$$\frac{dy}{dx} = (111x^2 + 74)(x^3 + 2x)^{36}$$



$$\frac{dy}{dx} = (111x^2 + 74)(x^3 + 2x)^{38}$$



What is the base of natural logarithm?

▶ **2.71**

▶ 10

▶ 5

▶ Any real number

Let  $x_0$  be critical points of the function  $f$ . Those critical points for which  $f'(x_0) = 0$  are called \_\_\_\_\_ of  $f$

▶ Local points

▶ End points

▶ **Stationary points**

The average velocity of a body is  $V_{ave}$

$$\frac{d_1 - d_0}{t_1 - t_0}$$



$$\frac{t_1 - t_0}{f(t_0) - f(t_1)}$$



$$\lim_{t_1 \rightarrow t_0} \frac{f(t_0) - f(t_1)}{t_1 - t_0}$$



▶ None of these

Consider two function  $f(x) = x^3$  and  $g(x) = (x+9)$  then  $f \circ g(x) =$

▶  $(x+9)^3$

▶  $x+3$

▶  $x+9$

▶ None of these

Consider two function  $f(x) = x^2$  and  $g(x) = \sqrt{x}$  then  $f \circ g(x) =$  .....

▶  $x$  -correct

▶  $x^2$

▶  $\sqrt{x}$

▶ None of these

Consider two function  $f(x) = 3\sqrt{x}$  and  $g(x) = \sqrt{x}$  what is true about these functions

▶  $f(x).g(x) = 3x$

$$\frac{f(x)}{g(x)} = 3x$$

- ▶
- ▶  $f(g(x)) = 3x$
- ▶ None of these -correct

The centre and the radius of the circle  $(x+5)^2 + (y-3)^2 = 16$  is

- ▶  **$(-5,3), 4$**
- ▶  $(5,-3), 16$
- ▶  $(5,-3), 4$
- ▶ None of these

The graph  $x = y^2$  is symmetric about

- ▶ **X-axis**
- ▶ Y-axis
- ▶ Origin
- ▶ None of these

The chain rule is used for two function f and g , if we have ----- of these function

- ▶ Product
- ▶ Sum
- ▶ **Composition**
- ▶ None of these

A function f is differentiable function if it is differentiable on the interval

- ▶  $(-\infty, \infty)$
- ▶  $(a, \infty)$  where  $a$  is any negative integer
- ▶  $(0, \infty)$
- ▶ None of these

A function is said to be continuous function if the function is continuous on the interval

- ▶  $(-\infty, +\infty)$
- ▶  $(0, +\infty)$
- ▶  $(-\infty, 0)$
- ▶ None of these

$$\lim_{x \rightarrow 0} \frac{\sin x}{x}$$

- ▶ 1
- ▶ 2
- ▶ 0-correct
- ▶ 1/2

For any polynomial  $P(x) = c_0 + c_1x + \dots + c_nx^n$  and any real number  $a$

$$\lim_{x \rightarrow a} P(x) = c_0 + c_1a + \dots + c_na^n =$$

- ▶  $P(a)$  -correct

▶  $P(a+1)$

▶  $P(a-1)$

▶  $\frac{1}{P(a)}$

▶

The no of x and y intercepts for the equation  $y=1/x$

▶ Two x intercepts

▶ Two y intercepts

▶ No x and no y intercepts-correct

▶ None of these

A line is called a tangent line to the circle if it meets the circle at precisely

▶ One point -correct

▶ Two points

▶ Infinite points

▶ None of these

If f is a twice differentiable function at a stationary point  $x_0$  and  $f''(x_0) < 0$

then f has relative ..... At  $x_0$

▶ Minima

▶ Maxima

▶ None of these

If the  $\lim_{x \rightarrow a} f(x) = L$  then the inequality  $(L - \varepsilon) < f(x) < L + \varepsilon$  holds in any subset of the interval

- ▶  $(a - \delta, a) \cup (a, a + \delta)$
- ▶  $(a - 1, a) \cup (a, a + 1)$
- ▶  $(a - \varepsilon, a) \cup (a, a + \varepsilon)$
- ▶ None of these

### Questions:

**Question No: 1 ( Marks: 10 )**

Evaluate the following limit.

$$\lim_{x \rightarrow 2} \frac{x^2 + 4x - 12}{x^2 - 2x}$$

**Question No: 2 ( Marks: 3 )**

Discuss the concavity of the function  $f(t) = (2-t)(t-3) + 3$  on any interval using second derivative test?

**Question No: 3 ( Marks: 5 )**

Find the derivative of the function  $y = \ln(1 + x^3)$

**Question No: 4 ( Marks: 10 )**

Compute derivative of trigonometric function  $\sin(x)$  by definition.

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