

Assignment# 01

MTH#202

Student id#bc240406390

Question #1 Use symbols to write the logical -----?

Solution:

Let A = Alice is a manager

B = Bob is a supervisor

Premise 1: if Alice is a manager, then Bob is not a supervisor.

$$A \rightarrow \neg B$$

Premise 2: if Bob is a supervisor, then Alice is not a manager.

$$B \rightarrow \neg A$$

Conclusion: Alice is not a manager, and Bob is not a supervisor.

$$\neg A \wedge \neg B$$

A	B	$\neg A$	$\neg B$	$A \rightarrow \neg B$	$B \rightarrow \neg A$	$\neg A \wedge \neg B$
T	T	F	F	F	F	F
T	F	F	T	T	T	F
F	T	T	F	T	T	F
F	F	T	T	T	T	T

Hence highlighted row all true so arguments is vailed.

Question#2: Prove that $A \setminus B = A \cap B^c$.

Solution:

Let $x \in A \setminus B$

By the definition of set difference.

$x \in A$ and x not belong to B

Since x not belong to B , it follows that $x \in B^c$.

Therefore, $x \in A$ and $x \in B^c$.

so $x \in A \cap B^c$.

Thus, $A \setminus B \subseteq A \cap B^c$.

Let $x \in A \cap B^c$

By the definition of intersection.

$x \in A$ and $x \in B^c$.

Since $x \in B^c$, we have x not belong to B .

Therefore, $x \in A$ and x not belong to B .

So, $x \in A \setminus B$ Thus,

$A \cap B^c \subseteq A \setminus B$.

Conclusion:

Since we have shown both $A \setminus B \subseteq A \cap B^c$ and $A \cap B^c \subseteq A \setminus B$,

We conclude that: $A \setminus B = A \cap B^c$.

Question#3: Out of 80 students in a -----?

Solution:

- C: Students who attended the Coding session.
- D: Students who attended the Data Science session.
- M: Students who attended the Machine Learning session.

$$|C \cap D| = 30$$

$$|D \cap M| = 25$$

$$|C \cap M| = 20$$

$$|C \cap D \cap M| = 10$$

$$|C \cup D \cup M| = |D| + |M| - |C \cap D| - |D \cap M| - |C \cap M| + |C \cap D \cap M|$$

$$80 = |C| + |D| + |M| - 30 - 25 - 20 + 10$$

$$2x + |M| = 145 \text{ ----- (1)}$$

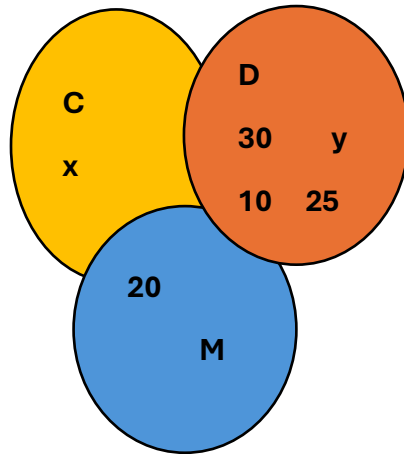
Here

$$|M| = 20 + 25 - 10 = 35$$

Put $|M|$ in eq 1

$$2x + 35 = 135$$

$$X = 55$$



Question#4: Consider the inequality -----?

Solution: $0 < x \leq \sqrt{2}$

$0 < x$ (which mean x is greater than 0)

$x \leq \sqrt{2}$ (which means x is less than or equal to $\sqrt{2}$).

Negation of $0 < x$ is $x \leq 0$

Negation of $x \leq \sqrt{2}$ is $x > \sqrt{2}$

By De Morgan's Laws, the negation of the compound statement $(0 < x \leq \sqrt{2})$ is the "or" combination of the negated parts:

$$x \leq 0 \text{ or } x > \sqrt{2}$$

The negation of $0 < x \leq \sqrt{2}$ is :

$$x \leq 0 \text{ or } x > \sqrt{2} \text{ is}$$

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